

# Validation of Radiance against CIE171:2006 and Improved Adaptive Subdivision of Circular Light Sources

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## CIE171:2006: Test Cases to Assess the Accuracy of Lighting Computer Programs

- proposed in 2006 by the International Commission on Illumination (CIE) in Publication 171:2006
- goal: assess accuracy of lighting computer programs and identify weaknesses
- experimental and analytical test cases

⇒ Possibility of comparison with AGI32 results published by Dau Design and Consulting Inc.

# Experimental Test Cases

## Overview

- based on experimental protocol of CIBSE TM 28/00 (Slater and Graves, 2002)
- real-world test scenes
- different luminaires and surface reflectances
- inaccuracy: dark brown floor (negligible for illuminances)

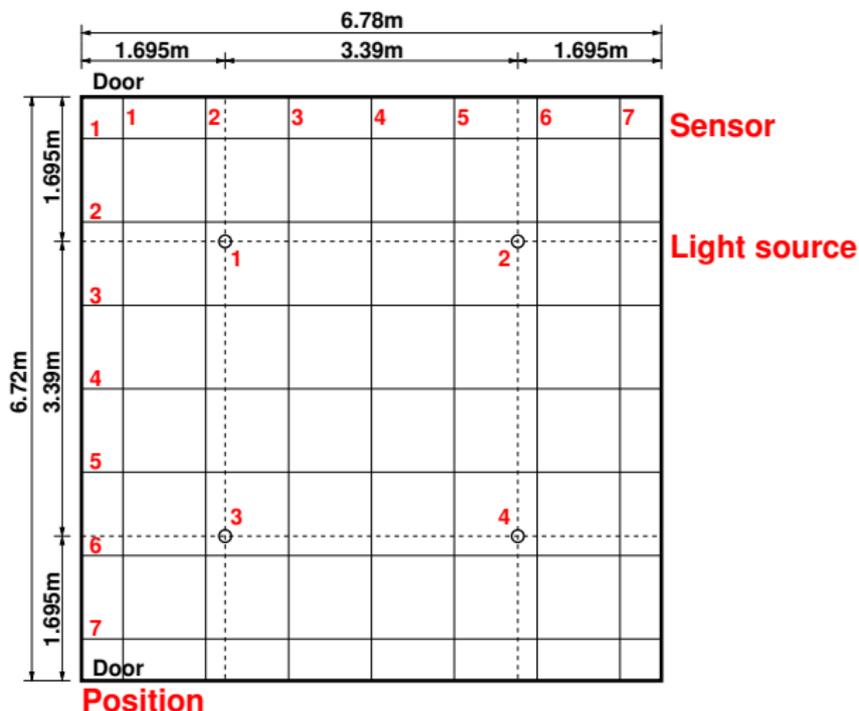
# Experimental Test Cases

## Measurements

- 49 measurement positions on a regular grid
- measurement plane 0.80m above the floor level
- measured variable: illuminance
- two measurement error bands for **point illuminances**:  
**measurement error** (+/- 2 x 6.7%) and  
**total error** (+/- 2 x 10.5%, including simulation errors)
- **room average illuminances**:  
**total expectation error** (measurement +/- 2 x 6.3%)

# Experimental Test Cases

## Measurement points



# Test Case 4.1: grey wall, CFL lamp

## Set-up

- ceiling: white acoustic tiles (70% reflectance)
- floor: dark brown (6% reflectance)
- walls: matte grey (41% reflectance)
- luminaires: compact fluorescent lamps modeled as **point light sources**; output ( $\approx 2200$  lm each) and photometric data given

Total expectation error upper limit	112.0
Radiance mean room illuminance	88.5
Total expectation error lower limit	88.0

# Test Case 4.1: grey wall, CFL lamp

## Set-up

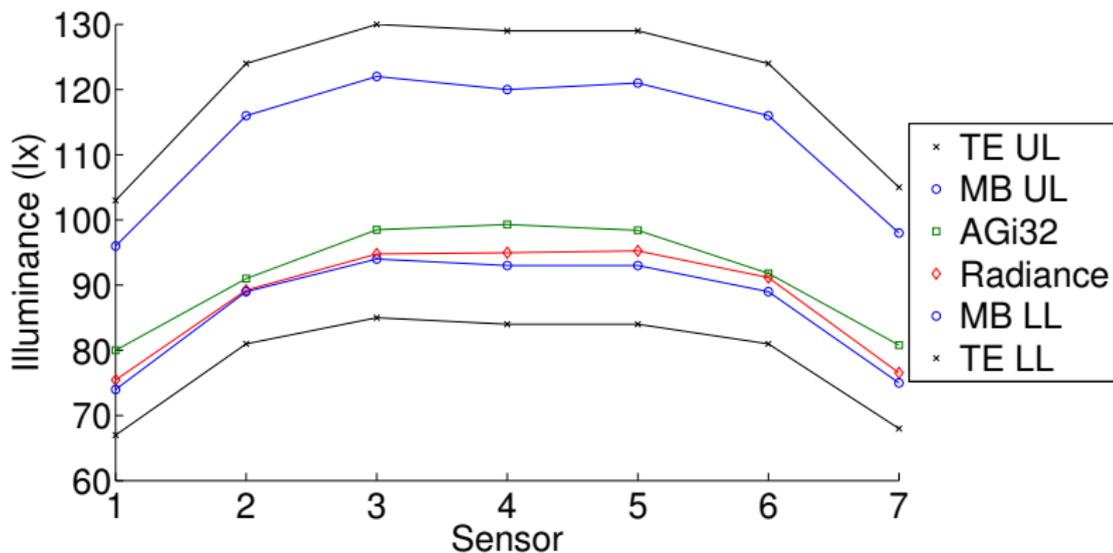
- ceiling: white acoustic tiles (70% reflectance)
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Total expectation error upper limit	112.0
<b>Radiance mean room illuminance</b>	<b>88.5</b>
Total expectation error lower limit	88.0

# TC 4.1: grey wall, CFL lamp

## Results (Position 2)

⇒ all 49 values inside measurement band (AGI32: 49)



# Test Case 4.2: grey wall, opal luminaire

## Set-up

- ceiling: white acoustic tiles (70% reflectance)
- floor: dark brown (6% reflectance)
- walls: matte grey (52% reflectance)
- light sources: 4 **circular luminaires** (450mm diameter) with compact fluorescent lamps; output ( $\approx$  1800 lm – 2100 lm each) and photometric data given

Total expectation error upper limit	67.5
Radiance mean room illuminance	51.4
Total expectation error lower limit	53.1

# Test Case 4.2: grey wall, opal luminaire

## Set-up

- ceiling: white acoustic tiles (70% reflectance)
- floor: dark brown (6% reflectance)
- walls: matte grey (52% reflectance)
- light sources: 4 **circular luminaires** (450mm diameter) with compact fluorescent lamps; output ( $\approx$  1800 lm – 2100 lm each) and photometric data given

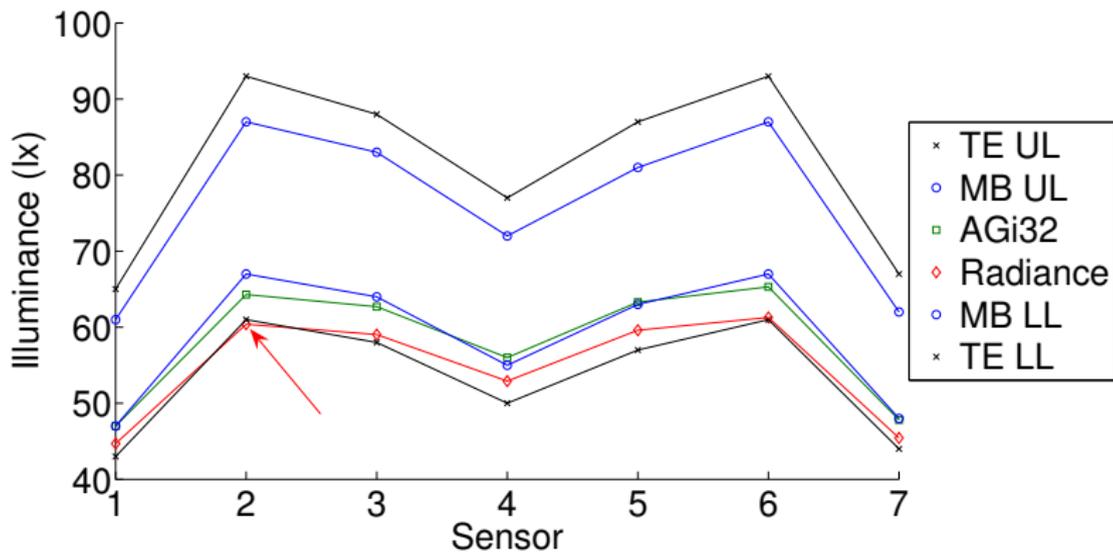
Total expectation error upper limit	67.5
<b>Radiance mean room illuminance</b>	<b>51.4</b>
Total expectation error lower limit	53.1

# TC 4.2: grey wall, opal luminaire

## Results (Position 2)

⇒ 33/49 values (67.35%) below MB LL (AGI32: 12)

⇒ 1 value even outside total error band (AGI32: 0)



# Test Case 4.3: grey wall, semi-specular reflector (SSR) luminaire

## Set-up

- ceiling: white acoustic tiles (70% reflectance)
- floor: dark brown (6% reflectance)
- walls: matte grey (52% reflectance)
- light sources: 4 **square luminaires** (600 mm × 600 mm) with compact fluorescent lamps; output ( $\approx$  4100 lm each) and photometric data given

Total expectation error upper limit	254.2
Radiance mean room illuminance	234.5
Total expectation error lower limit	199.8

# Test Case 4.3: grey wall, semi-specular reflector (SSR) luminaire

## Set-up

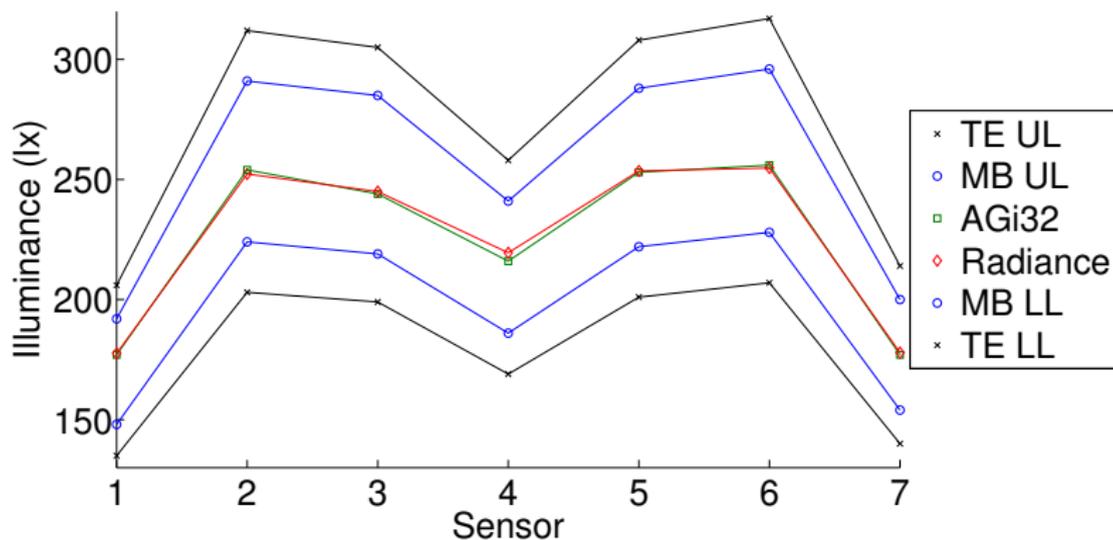
- ceiling: white acoustic tiles (70% reflectance)
- floor: dark brown (6% reflectance)
- walls: matte grey (52% reflectance)
- light sources: 4 **square luminaires** (600 mm × 600 mm) with compact fluorescent lamps; output ( $\approx$  4100 lm each) and photometric data given

Total expectation error upper limit	254.2
<b>Radiance mean room illuminance</b>	<b>234.5</b>
Total expectation error lower limit	199.8

# TC 4.3: grey wall, SSR luminaire

## Results (Position 2)

⇒ all 49 values inside measurement band (AGI32: 49)



# Test Cases with Analytical References

## Overview

- lighting simulations based on theoretical, physical laws

### Goals:

- isolate certain aspects of the light propagation
- minimize / eliminate uncertainty in the reference values

# Test Case 5.6: Light reflection over diffuse surfaces

## Specification

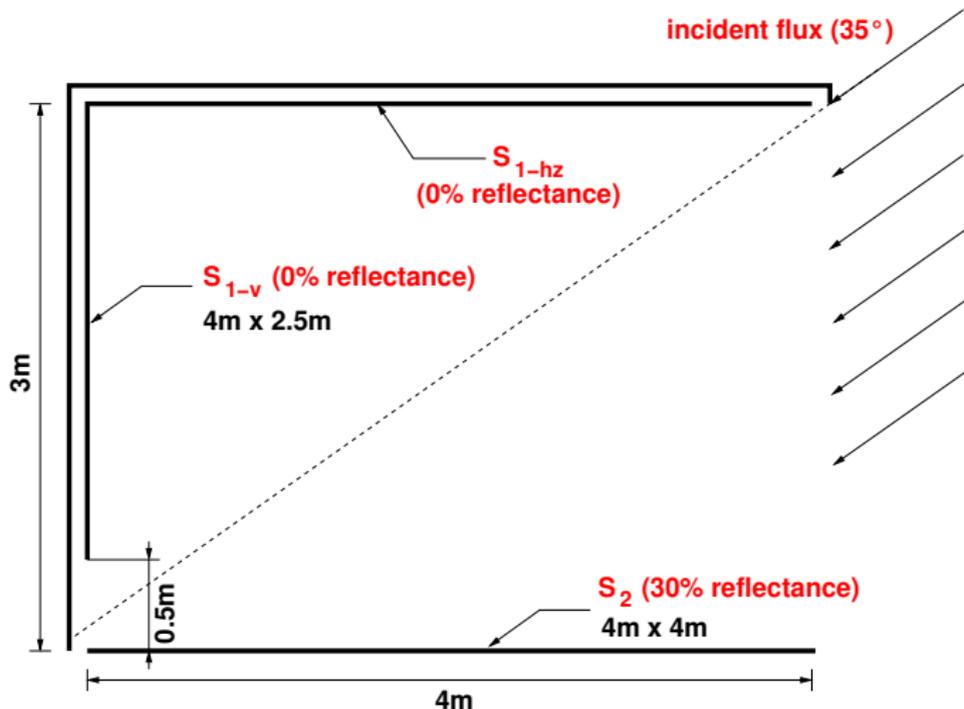
- reflection of light inside a room
- reflection of daylight on the external ground
- 4m×4m reflecting surface, 30% reflectance
- measured variable: relative illuminance divided by reflectance

$$E / (E_{hz} \cdot \rho)$$

(equal to configuration factor  $F_{12}$  between the measurement point and the reflecting surface  $S_2$ )

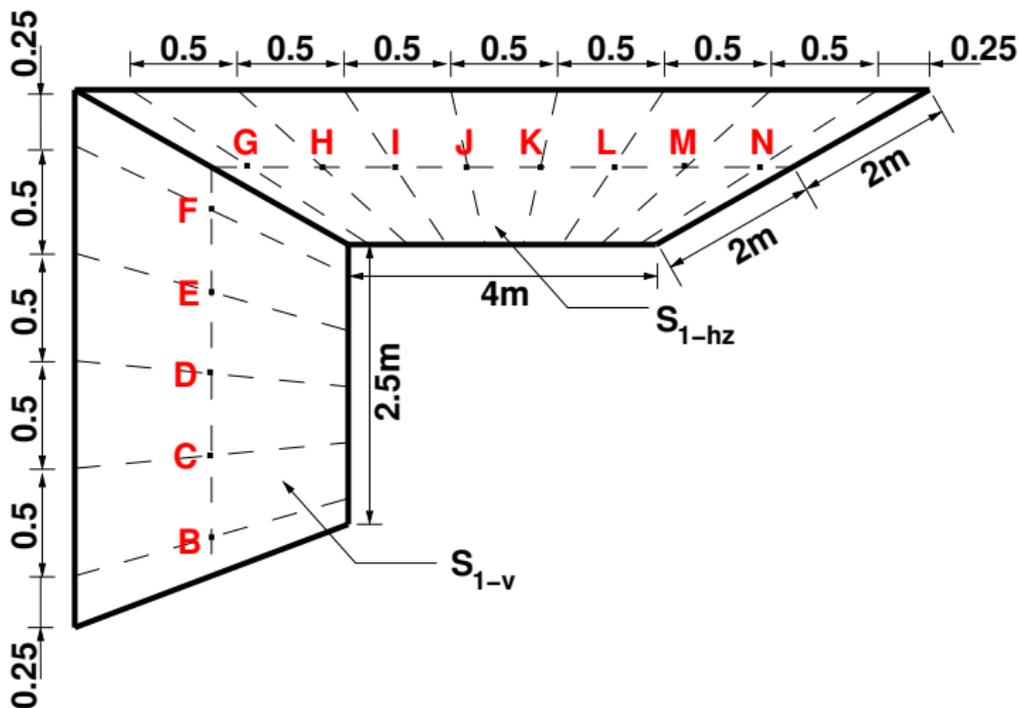
# TC 5.6: Light reflection over diffuse surfaces

## Test scene description



# TC 5.6: Light reflection over diffuse surfaces

## Measurement points



# TC 5.6: Light reflection over diffuse surfaces

## Results

	Points of measurement for $S_{1-v}$				
$F_{12}$	B	C	D	E	F
CIE Reference	35.901	27.992	21.639	16.716	12.967
<b>Radiance</b>	<b>35.861</b>	<b>27.898</b>	<b>21.573</b>	<b>16.707</b>	<b>12.955</b>

Points of measurement for $S_{1-hz}$							
G	H	I	J	K	L	M	N
26.80	30.94	33.98	35.57	35.57	33.98	30.94	26.80
<b>26.77</b>	<b>30.91</b>	<b>33.94</b>	<b>35.53</b>	<b>35.53</b>	<b>33.94</b>	<b>30.91</b>	<b>26.77</b>

mean error: 0.137%

# Test Case 5.7: Diffuse reflection with internal obstructions

## Specification

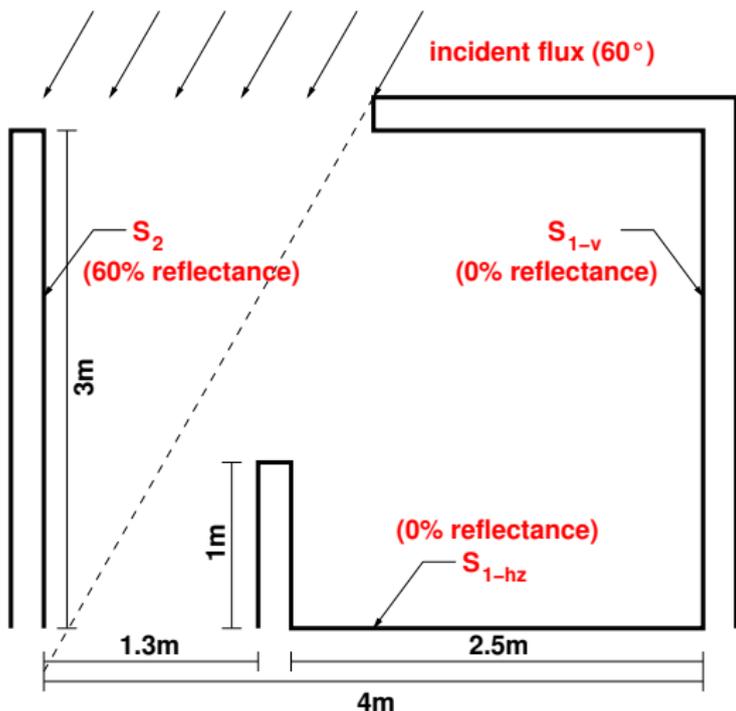
- **influence of an obstruction** to diffuse reflection
- shading influence of internal furniture
- externally reflected component received from external objects through apertures
- measured variable: relative illuminance divided by reflectance

$$E / (E_{hz} \cdot \rho)$$

(equal to configuration factor  $F_{12}$  between the measurement point and the unobstructed portion of the reflecting surface  $S_2$ )

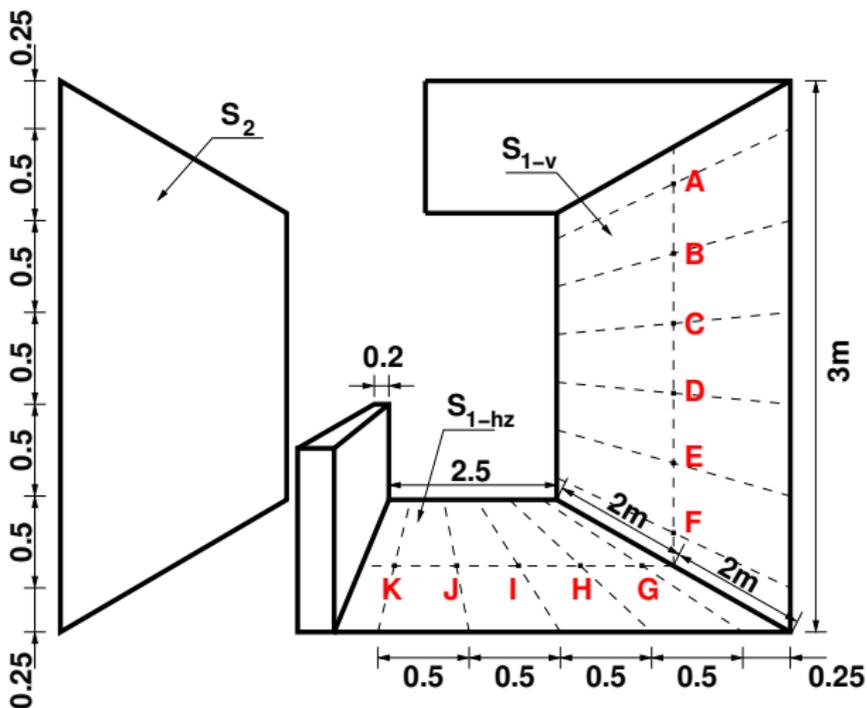
# TC 5.7: Diffuse reflection with internal obstructions

## Test scene description



# TC 5.7: Diffuse reflection with internal obstructions

## Measurement points



# TC 5.7: Diffuse reflection with internal obstructions

## Results

	Points of measurement for $S_{1-v}$					
$F_{12}$	A	B	C	D	E	F
CIE Reference	20.941	21.187	19.946	17.284	14.053	9.751
<b>Radiance</b>	<b>16.096</b>	<b>16.359</b>	<b>15.422</b>	<b>13.332</b>	<b>10.310</b>	<b>7.077</b>

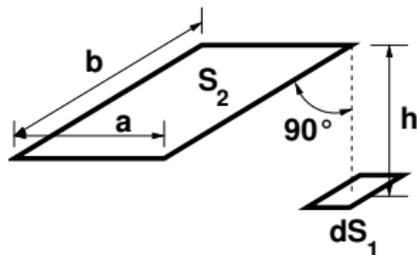
	Points of measurement for $S_{1-hz}$				
$F_{12}$	G	H	I	J	K
CIE Reference	4.761	5.261	4.535	0.000	0.000
<b>Radiance</b>	<b>3.366</b>	<b>3.615</b>	<b>3.012</b>	<b>0.000</b>	<b>0.000</b>

**mean error: 21.791%**

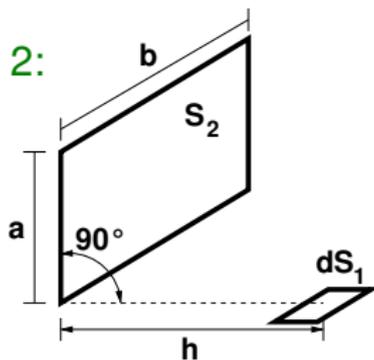
# TC 5.7: Diffuse reflection with internal obstructions

Analytical calculation of configuration factors

Case 1:



Case 2:



$$1: F_{12} = \frac{1}{2\pi} \cdot \left[ \frac{X}{\sqrt{1+X^2}} \cdot \arctan \frac{Y}{\sqrt{1+X^2}} + \frac{Y}{\sqrt{1+Y^2}} \cdot \arctan \frac{X}{\sqrt{1+Y^2}} \right]$$

$$2: F_{12} = \frac{1}{2\pi} \cdot \left[ \arctan Y - \frac{1}{\sqrt{1+X^2}} \cdot \arctan \frac{Y}{\sqrt{1+X^2}} \right]$$

where  $X = \frac{a}{h}$  and  $Y = \frac{b}{h}$

# TC 5.7: Diffuse reflection with internal obstructions

## Results

	Points of measurement for $S_{1-v}$					
$F_{12}$	A	B	C	D	E	F
CIE Reference	20.941	21.187	19.946	17.284	14.053	9.751
analytical	16.071	16.330	15.399	13.322	10.317	7.079
Radiance	16.096	16.359	15.422	13.332	10.310	7.077

	Points of measurement for $S_{1-hz}$				
$F_{12}$	G	H	I	J	K
CIE Reference	4.761	5.261	4.535	0.000	0.000
analytical	3.382	3.629	3.013	0.000	0.000
Radiance	3.366	3.615	3.012	0.000	0.000

mean error (analytical ↔ Radiance): 0.142%

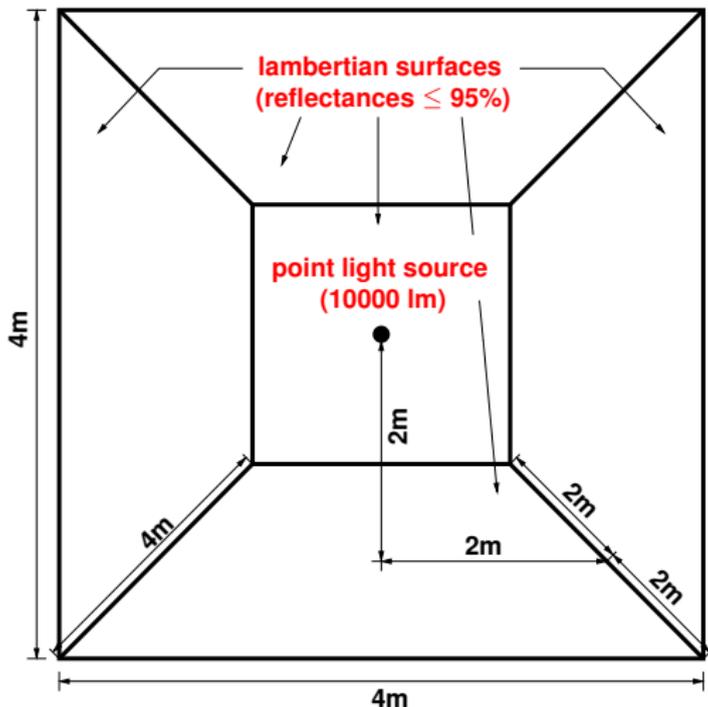
# Test Case 5.8: Internal reflected component calculation for diffuse surfaces

## Specification

- **diffuse interreflections** inside a room
- contribution of interreflections to global illumination inside a room
- measured variable: average indirect illuminance  $E_{av}$

# TC 5.8: Internal reflected component calculation

## Test scene description



# TC 5.8: Internal reflected component calculation

## Results

	Indirect average illuminance variation					
Reflectance	0%	5%	10%	20%	30%	40%
$E_{av}(lx)$ CIE	0.00	5.48	11.6	26.0	44.6	69.4
<b>Radiance</b>	<b>0.00</b>	<b>5.50</b>	<b>11.5</b>	<b>26.0</b>	<b>44.6</b>	<b>69.7</b>

	Indirect average illuminance variation					
Reflectance	50%	60%	70%	80%	90%	95%
$E_{av}(lx)$ CIE	104	156	243	417	937	1979
<b>Radiance</b>	<b>104</b>	<b>157</b>	<b>244</b>	<b>419</b>	<b>884</b>	<b>1472</b>

mean error for reflectances  $\leq 80\%$ : 0.318%

# Validation of Radiance against CIE171:2006

## Conclusion

- good results for experimental test cases with **point** and **square light sources** (test cases 4.1 and 4.3)
- weakness in modeling **circular light sources** (test case 4.2)
- error in CIE references for test case 5.7
- proper modeling of **diffuse reflection** (test cases 5.6, 5.7 and 5.8)
- lambertian surfaces with reflectances  $> 80\%$  problematic (test case 5.8; slow convergence of Neumann series for the solution of Kajiya's rendering equation used in ray tracing)

# Motivation

## Experimental test case 4.2:

4 circular luminaires (450mm diameter) with CFLs

Total expectation error upper limit	67.5
<b>Radiance mean room illuminance</b>	<b>51.4</b>
Total expectation error lower limit	53.1

⇒ 33/49 values (67.35%) below measurement band lower limit

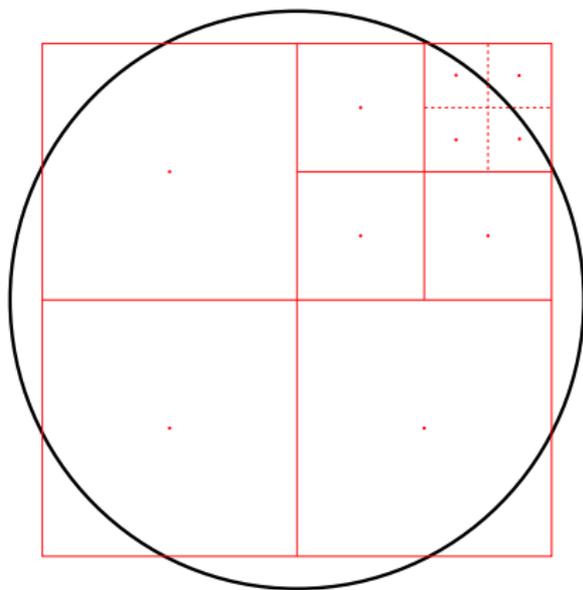
⇒ 1 value even outside total error band

# Current Implementation

## Radiance:

(Ward and Shakespeare, 1998)

- all flat light sources approximated as **rectangles**
- circular light source approximated as square
- jittering over full source volume: probability for **aiming failure: 9.1%**
- full subdivision, no jittering: 4 out of 64 rays miss light source



# Current Implementation

## Subdivision algorithm:

- if fraction (source size  $\div$  distance to source) too large ( $-ds$  option), subdivide along longest axis
- repeat on each subsource until size criterion is satisfied

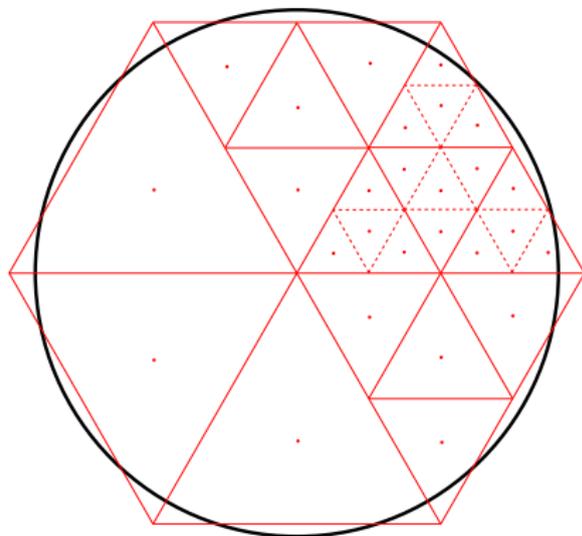
## Jittering:

- jitter over rectangular volumes
- degree of jittering controlled by  $-dj$  option

# Triangulation approach

## Improved subdivision:

- approximate circular light source as **hexagon**
- subdivide hexagon into equilateral triangles
- jittering over full source volume: probability for *aiming failure decreases from 9.1% to 3.7%*
- full subdivision, no jittering: all 96 rays hit light source



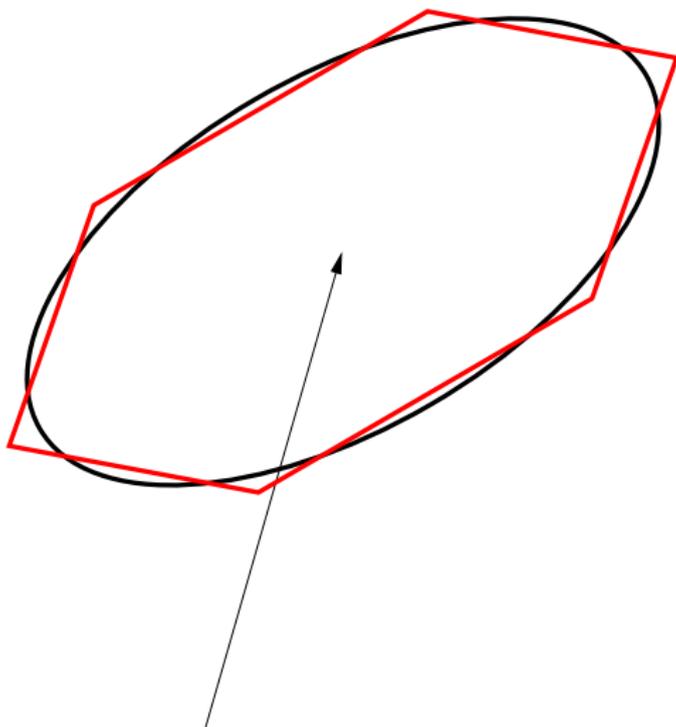
# Triangulation approach

## Subdivision algorithm:

```
RINGPART(srcindex si, ray r)
  initialize;
  if ((source size ÷ distance to source) too small)
    no subdivision;
    return ;
  approximate disk as hexagon;
  subdivide into 6 equilateral triangles;
  for each triangle
    while ((partition size ÷ distance to current partition) too large)
      subdivide into 4 equilateral triangles;
  write partition structure to si;
```

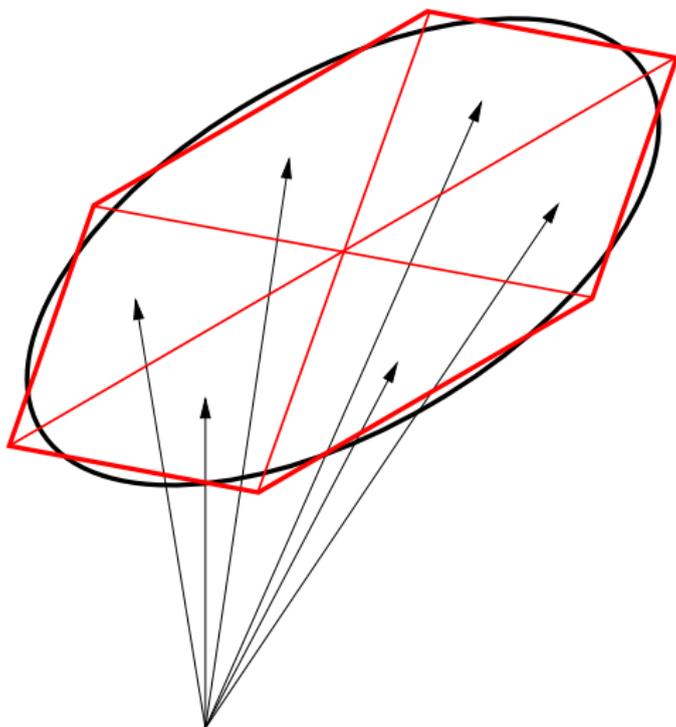
# Triangulation approach

## Subdivision algorithm



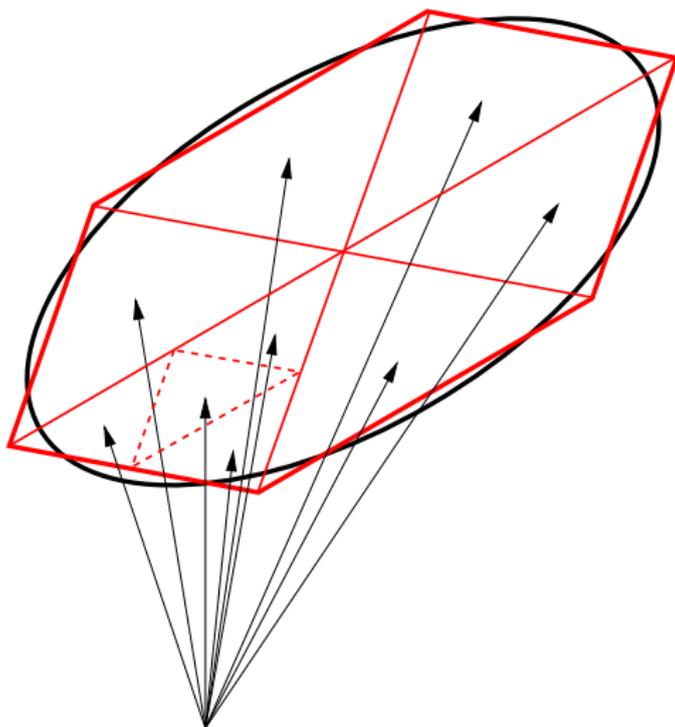
# Triangulation approach

## Subdivision algorithm



# Triangulation approach

## Subdivision algorithm



# Triangulation approach

## Jittering:

- if source is not subdivided: circular jittering (Shirley, Wang and Zimmermann, 1996)
- if source is subdivided: triangular jittering based on barycentric coordinates
- degree of jittering controlled by  $-dj$  option as in the standard algorithm

# Triangulation approach

## Implementation:

- definition of macro SRING in *src/rt/source.h*
- additional functions `ringpart`, `flt_tripartit` and `skiptriparts` in *src/rt/srcsamp.c*  
(similar to `flatpart`, `flt_partit` and `skipparts`)
- additional vector operations defined in *src/common/fvect.h*
- minor changes to *src/rt/srcsupp.c*

# Triangulation approach – Results

Analytical test: illuminance under a totally diffuse circular light source

## Analytical:

$$E = L_0 \pi \frac{r^2}{r^2 + h^2} = \frac{\Phi}{\pi(r^2 + h^2)}$$

$$= \mathbf{124.705 \text{ lux}}$$

## Radiance:

(64 quads, aiming failure!)

$$E = \mathbf{117.082 \text{ lux}}$$

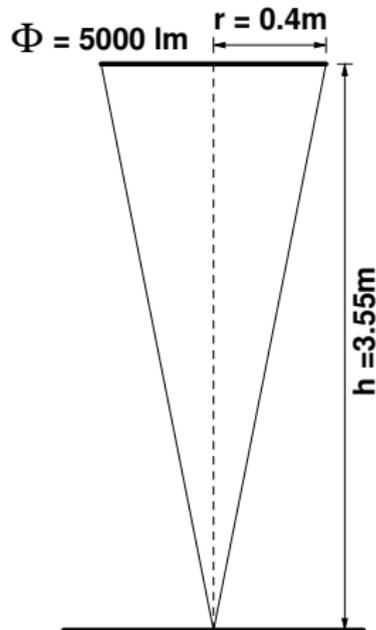
$$\text{Error} = \mathbf{6.11\%}$$

## Triangulation approach

(96 triangles):

$$E = \mathbf{124.800 \text{ lux}}$$

$$\text{Error} = \mathbf{0.08\%}$$



# Triangulation approach – Results

TC 4.2: grey wall, opal luminaire

## Experimental test case 4.2:

4 circular luminaires (450mm diameter) with CFLs

Simulated mean room illuminance	
Total expectation error upper limit	67.5
<b>Radiance</b>	<b>51.4</b>
<b>Triangulation approach</b>	<b>54.0</b>
Total expectation error lower limit	53.1

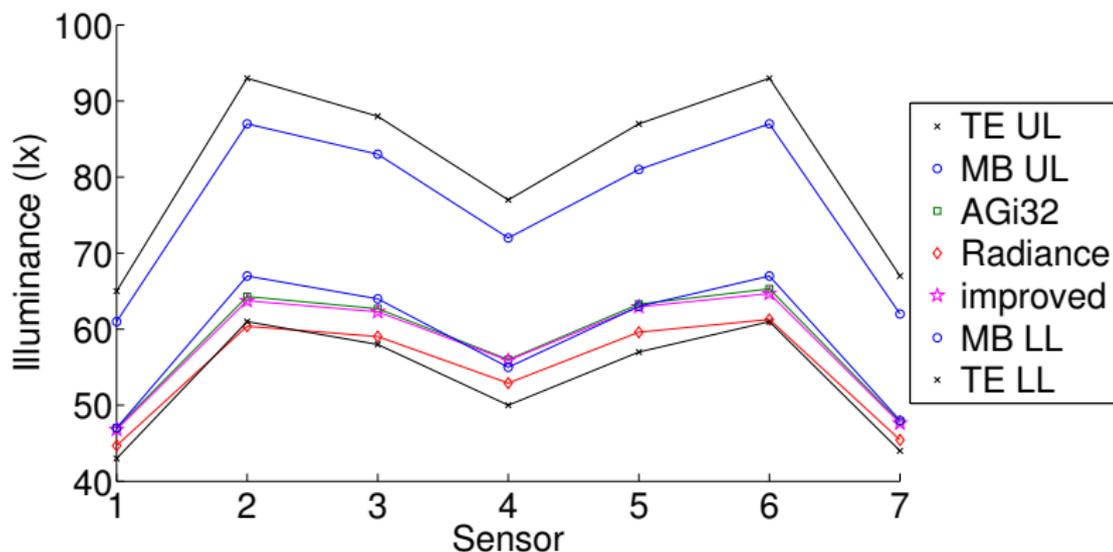
- ⇒ 33/49 values (67.35%) below measurement lower limit
- ⇒ 1 of those values even outside total error band
- ⇒ 12/49 values (24.49%) below measurement lower limit  
(63.64% decrease of values below limit)
- ⇒ all 49 calculated values inside total error band
- ⇒ mean illuminance increase of 5.23%

# Triangulation approach – Results

TC 4.2: grey wall, opal luminaire; position 2

⇒ 12/49 values (24.49%) below MB LL (AGI32: 12)

⇒ all 49 values inside total error band (AGI32: 49)



# Triangulation approach – Results

Real world test scene – seminar room at Lichtakademie Bartenbach



# Triangulation approach – Results

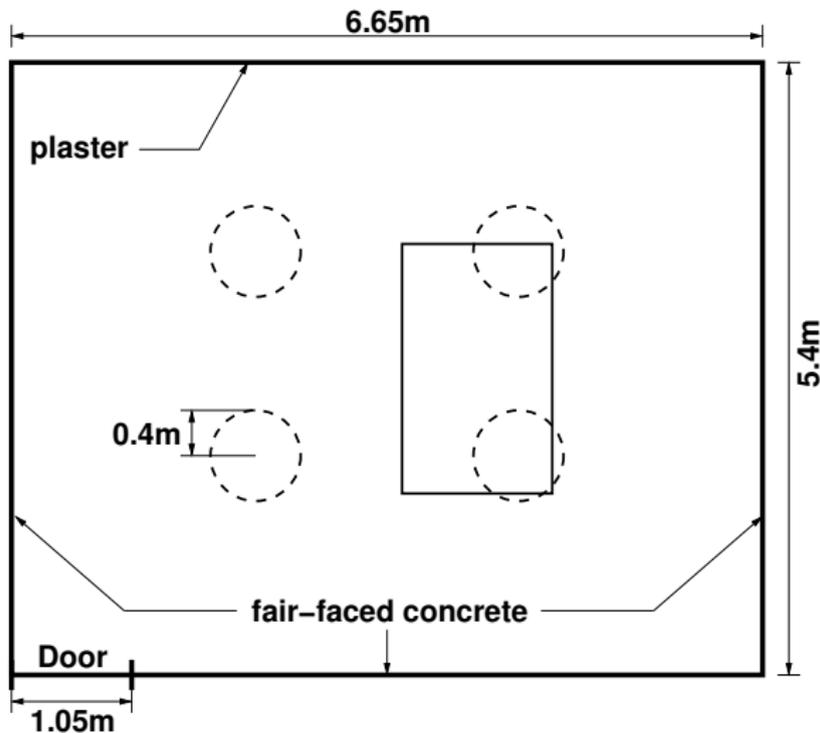
Real world test scene – seminar room at Lichtakademie Bartenbach

## Simplified set up

- red linoleum floor, 3 fair-faced concrete walls, 1 plastered wall, plastered ceiling
- 4 light tubes with scattering inserts
- spectral measurements of reflectances and photometric data of light sources done by Bartenbach LichtLabor

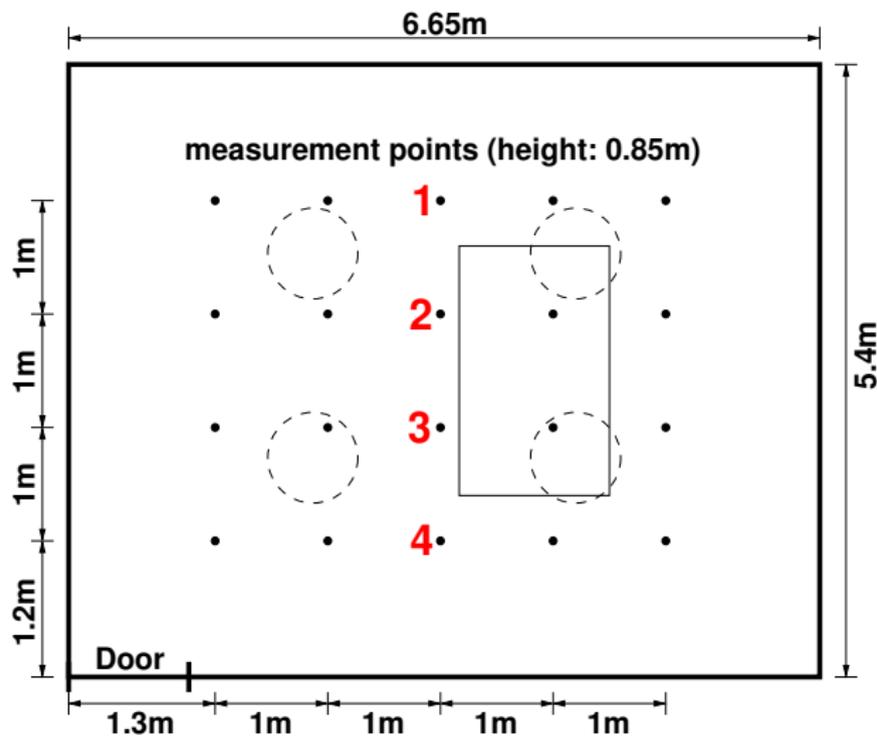
# Triangulation approach – Results

Seminar room: simplified set up



# Triangulation approach – Results

Seminar room: simplified set up (measurement points)



# Triangulation approach – Results

Real world test scene – seminar room at Lichtakademie Bartenbach

Measurement point	1	2	3	4
Measurement	600.2	844.4	819.4	560.2
<b>Radiance</b>	<b>621.0</b>	<b>776.9</b>	<b>739.7</b>	<b>515.6</b>
<i>Deviance</i>	3.47%	7.99%	9.73%	7.96%
<b>Triangulation approach</b>	<b>657.9</b>	<b>825.9</b>	<b>786.8</b>	<b>546.6</b>
<i>Deviance</i>	9.61%	2.19%	3.98%	2.43%

- mean decrease in deviance: **-2.74%**
- mean illuminance increase from Radiance to our triangulation approach: **+ 6.16%**
- probable reason for deviances: imprecise modeling of light tubes with scattering inserts

# Improved Adaptive Subdivision of Circular Light Sources

## Conclusion

- significant improvement in **accuracy**  
Analytical test: error decrease from 6.11% to 0.08%  
Test case 4.2: all values inside total error band  
Seminar room: mean deviance decrease of 2.74%
- measured **illuminance increase of about 6%**
- only slight increase in **rendering time** (about 0% – 5%)

# Acknowledgment

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# References

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**Any questions?**